

NAG C Library Function Document

nag_zhptri (f07pwc)

1 Purpose

nag_zhptri (f07pwc) computes the inverse of a complex Hermitian indefinite matrix A , where A has been factorized by nag_zhptrf (f07prc), using packed storage.

2 Specification

```
void nag_zhptri (Nag_OrderType order, Nag_UploType uplo, Integer n, Complex ap[],
               const Integer ipiv[], NagError *fail)
```

3 Description

To compute the inverse of a complex Hermitian indefinite matrix A , this function must be preceded by a call to nag_zhptrf (f07prc), which computes the Bunch–Kaufman factorization of A using packed storage.

If **uplo** = **Nag_Upper**, $A = PUDU^H P^T$ and A^{-1} is computed by solving $U^H P^T XPU = D^{-1}$ for X .

If **uplo** = **Nag_Lower**, $A = PLDL^H P^T$ and A^{-1} is computed by solving $L^H P^T XPL = D^{-1}$ for X .

4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* **12** 1–19

5 Parameters

- 1: **order** – Nag_OrderType *Input*
On entry: the **order** parameter specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = **Nag_RowMajor**. See Section 2.2.1.4 of the Essential Introduction for a more detailed explanation of the use of this parameter.
Constraint: **order** = **Nag_RowMajor** or **Nag_ColMajor**.
- 2: **uplo** – Nag_UploType *Input*
On entry: indicates how A has been factorized as follows:
 if **uplo** = **Nag_Upper**, $A = PUDU^H P^T$, where U is upper triangular;
 if **uplo** = **Nag_Lower**, $A = PLDL^H P^T$, where L is lower triangular.
Constraint: **uplo** = **Nag_Upper** or **Nag_Lower**.
- 3: **n** – Integer *Input*
On entry: n , the order of the matrix A .
Constraint: $n \geq 0$.
- 4: **ap**[*dim*] – Complex *Input/Output*
Note: the dimension, *dim*, of the array **ap** must be at least $\max(1, n \times (n + 1)/2)$.
On entry: details of the factorization of A stored in packed form, as returned by nag_zhptrf (f07prc).
On exit: the factorization is overwritten by the n by n Hermitian matrix A^{-1} stored in packed form.

- 5: **ipiv**[*dim*] – const Integer *Input*
Note: the dimension, *dim*, of the array **ipiv** must be at least $\max(1, \mathbf{n})$.
On entry: details of the interchanges and the block structure of *D*, as returned by nag_zhptrf (f07prc).
- 6: **fail** – NagError * *Output*
The NAG error parameter (see the Essential Introduction).

6 Error Indicators and Warnings

NE_INT

On entry, **n** = $\langle value \rangle$.
Constraint: **n** ≥ 0 .

NE_SINGULAR

The block diagonal matrix *D* is exactly singular.

NE_ALLOC_FAIL

Memory allocation failed.

NE_BAD_PARAM

On entry, parameter $\langle value \rangle$ had an illegal value.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

7 Accuracy

The computed inverse *X* satisfies a bound of the form

if **uplo** = **Nag_Upper**, $|DU^T P^T XPU - I| \leq c(n)\epsilon(|D||U^T|P^T|X|P|U| + |D||D^{-1}|)$;

if **uplo** = **Nag_Lower**, $|DL^T P^T XPL - I| \leq c(n)\epsilon(|D||L^T|P^T|X|P|L| + |D||D^{-1}|)$,

$c(n)$ is a modest linear function of *n*, and ϵ is the *machine precision*.

8 Further Comments

The total number of real floating-point operations is approximately $\frac{8}{3}n^3$.

The real analogue of this function is nag_dsptri (f07pjc).

9 Example

To compute the inverse of the matrix *A*, where

$$A = \begin{pmatrix} -1.36 + 0.00i & 1.58 + 0.90i & 2.21 - 0.21i & 3.91 + 1.50i \\ 1.58 - 0.90i & -8.87 + 0.00i & -1.84 - 0.03i & -1.78 + 1.18i \\ 2.21 + 0.21i & -1.84 + 0.03i & -4.63 + 0.00i & 0.11 + 0.11i \\ 3.91 - 1.50i & -1.78 - 1.18i & 0.11 - 0.11i & -1.84 + 0.00i \end{pmatrix}.$$

Here *A* is Hermitian indefinite, stored in packed form, and must first be factorized by nag_zhptrf (f07prc).

9.1 Program Text

```

/* nag_zhptri (f07pwc) Example Program.
 *
 * Copyright 2001 Numerical Algorithms Group.
 *
 * Mark 7, 2001.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf07.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Integer ap_len, i, j, n;
    Integer exit_status=0;
    NagError fail;
    Nag_UploType uplo_enum;
    Nag_OrderType order;

    /* Arrays */
    Integer *ipiv=0;
    char uplo[2];
    Complex *ap=0;

#ifdef NAG_COLUMN_MAJOR
#define A_UPPER(I,J) ap[J*(J-1)/2 + I - 1]
#define A_LOWER(I,J) ap[(2*n-J)*(J-1)/2 + I - 1]
    order = Nag_ColMajor;
#else
#define A_LOWER(I,J) ap[I*(I-1)/2 + J - 1]
#define A_UPPER(I,J) ap[(2*n-I)*(I-1)/2 + J - 1]
    order = Nag_RowMajor;
#endif

    INIT_FAIL(fail);
    Vprintf("f07pwc Example Program Results\n\n");

    /* Skip heading in data file */
    Vscanf("%*[\n] ");
    Vscanf("%ld%*[\n] ", &n);
    ap_len = n * (n + 1)/2;

    /* Allocate memory */
    if ( !(ipiv = NAG_ALLOC(n, Integer)) ||
        !(ap = NAG_ALLOC(ap_len, Complex)) )
    {
        Vprintf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    /* Read A from data file */
    Vscanf(" ' %1s '%*[\n] ", uplo);
    if (*(unsigned char *)uplo == 'L')
        uplo_enum = Nag_Lower;
    else if (*(unsigned char *)uplo == 'U')
        uplo_enum = Nag_Upper;
    else
    {
        Vprintf("Unrecognised character for Nag_UploType type\n");
        exit_status = -1;
        goto END;
    }
    if (uplo_enum == Nag_Upper)
    {
        for (i = 1; i <= n; ++i)
        {

```

```

        for (j = i; j <= n; ++j)
            Vscanf(" ( %lf , %lf )", &A_UPPER(i,j).re, &A_UPPER(i,j).im);
    }
    Vscanf("%*[^\\n] ");
}
else
{
    for (i = 1; i <= n; ++i)
    {
        for (j = 1; j <= i; ++j)
            Vscanf(" ( %lf , %lf )", &A_LOWER(i,j).re, &A_LOWER(i,j).im);
    }
    Vscanf("%*[^\\n] ");
}

/* Factorize A */
f07prc(order, uplo_enum, n, ap, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07prc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Compute inverse of A */
f07pwc(order, uplo_enum, n, ap, ipiv, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from f07pwc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
/* Print inverse */
x04ddc(order, uplo_enum, Nag_NonUnitDiag, n, ap,
        Nag_BracketForm, "%7.4f", "Inverse", Nag_IntegerLabels,
        0, Nag_IntegerLabels, 0, 80, 0, 0, &fail);
if (fail.code != NE_NOERROR)
{
    Vprintf("Error from x04ddc.\\n%s\\n", fail.message);
    exit_status = 1;
    goto END;
}
END:
    if (ipiv) NAG_FREE(ipiv);
    if (ap) NAG_FREE(ap);

return exit_status;
}

```

9.2 Program Data

f07pwc Example Program Data

```

4                                     :Value of N
'L'                                 :Value of UPLO
(-1.36, 0.00)
( 1.58,-0.90) (-8.87, 0.00)
( 2.21, 0.21) (-1.84, 0.03) (-4.63, 0.00)
( 3.91,-1.50) (-1.78,-1.18) ( 0.11,-0.11) (-1.84, 0.00) :End of matrix A

```

9.3 Program Results

f07pwc Example Program Results

Inverse	1	2	3	4
1	(0.0826, 0.0000)			
2	(-0.0335, 0.0440)	(-0.1408, 0.0000)		
3	(0.0603,-0.0105)	(0.0422,-0.0222)	(-0.2007,-0.0000)	
4	(0.2391,-0.0926)	(0.0304, 0.0203)	(0.0982,-0.0635)	(0.0073, 0.0000)